

Master's program Entrance examination topics

Mathematics

- 1. Real numbers. Sequences and series of numbers. Complex numbers.
- 2. Functions of real variable. Derivative. Taylor's formula.
- 3. Riemann integral of a function. Fundamental theorem of calculus. Newton-Leibniz's formula.
- 4. Differential equations. Linear systems.
- 5. Power series. Taylor's expansion. Trigonometric series.
- 6. Functions of more independent variables. Continuity and limits. Differentiability and partial derivatives. Taylor's theorem. Maximum and minimum values.
- 7. The Fourier integral. Inverse Fourier transform. Time- and frequency domain descriptions.
- 8. Complex functions. Line integral of complex functions. Zeros and poles.
- 9. Vector spaces. Linearly Independent Sets, Bases. Coordinate Systems. Dimension.
- 10. Vector algebra. 2d and 3d Vectors: Inner Product, Cross-Product, Mixed Product.
- 11. Matrix Operations: addition, multiplication, transpose. Inverse of a Matrix.
- 12. Vector Equations of a linear system of equations. The Matrix Equation Ax = b
- 13. Determinants. Applications: Area, Volume and Determinants. Cramer's Rule.
- 14. Representing Graphs, Graph Isomorphism. Euler and Hamilton Circles. Trees.
- 15. Propositional calculus. Basic and derived argument forms.
- 16. Cardinality of Sets and Subsets. Countable and uncountable sets. Continuum Cardinality.
- 17. Combinatorics: Counting Problems, Permutations, Combinations, Binomial Theorem
- 18. Probability, Discrete and Continuous Random Variables, Expected Value, Variance

Recommended literature:

- R. Courant F. John: *Introduction to Calculus and Analysis I-II*. Springer.
- D. C. Lay: Linear Algebra and Its Applications. University of Maryland, Pearson.
- K. H. Rosen: Discrete Mathematics with Applications. Mcgraw Hill.
- J. Stewart Daniel K. Clegg Saleem Watson: Multivariable Calculus. ISBN-13: 9780357439432
- D. P. Apte: Probability and Combinatorics. ISBN: 8174465200